

Traversable wormholes

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Overview

“Traversable wormhole via a double trace deformation”

[Gao, Jafferis and Wall, 1608.05687]

“Diving into traversable wormholes”

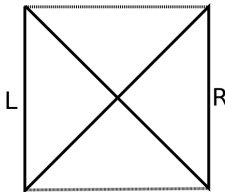
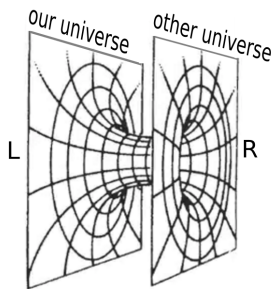
[Maldacena, Stanford and Yang, 1704.05333]

Work in progress

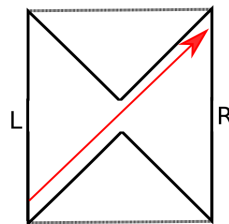
[with Elena Caceres and Minglei Xiao]

Traversable wormholes

Wormhole: A "throat" connecting two universes or a shortcut connecting two distant places in the same universe



non-traversable
wormhole



traversable
wormhole

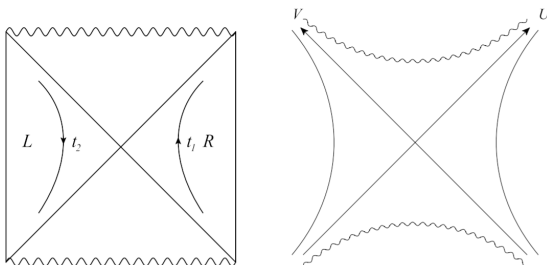
Traversable wormholes: Usually require addition of exotic matter, which violates energy conditions.

Framework: Embedded in AdS/CFT

BTZ black hole [Banados, Teitelboim, Zanelli '92]

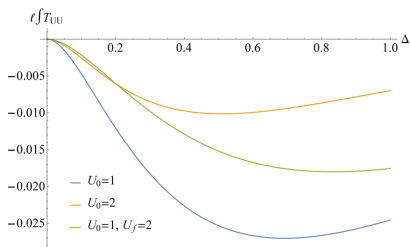
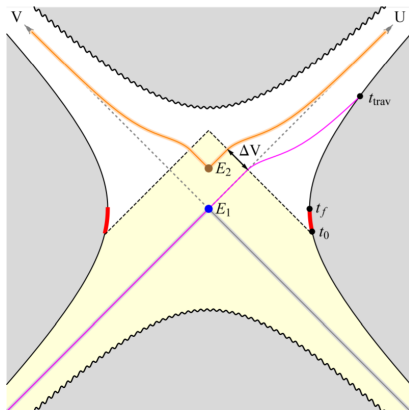
$$ds^2 = -\frac{r^2 - r_h^2}{\ell^2} dt^2 + \frac{\ell^2}{r^2 - r_h^2} dr^2 + r^2 d\phi^2, \quad \phi \sim \phi + 2\pi$$

Kruskal coordinates: $e^{2r_h t} = -\frac{U}{V}$, $\frac{r}{r_h} = \frac{1-UV}{1+UV}$



Constructing a traversable wormhole

Integration of T_{UU} is negative with appropriate choice of sign of the coupling h .



Linearized Einstein equation

$$V(U) \sim \int dU T_{UU}$$

Negative null energy $\Rightarrow$ Traversability

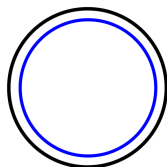
$$\Delta V \sim \frac{h G_N}{R^{D-2}}$$

Maldacena, Stanford and Yang

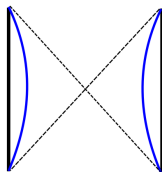
Dilaton gravity in 2D. Jackiw-Teiteboim theory

$$I_{JT} = \frac{1}{16\pi G_N} \left[\int d^2x \Phi \sqrt{g} (R + 2) + 2 \int_{bdy} \Phi_b K \right]$$

- Equation of motion for Φ : $R + 2 = 0 \Rightarrow$ Rigid AdS_2 geometry
- Dynamics is encoded in the boundary



Euclidean
 AdS_2



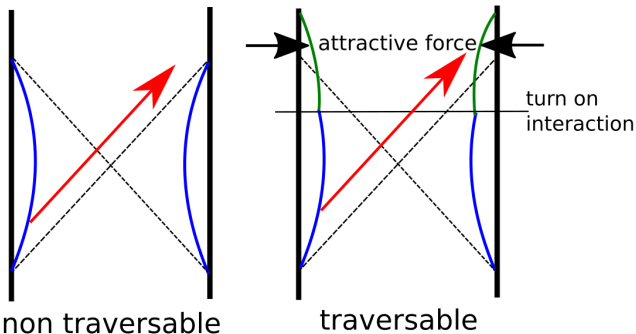
Lorentzian
 AdS_2 black hole
(Rindler)

Blue lines:
boundary cutoffs

Maldacena, Stanford and Yang

$$e^{i\tilde{g}V} = e^{i\tilde{g}\mathcal{O}_L(0)\mathcal{O}_R(0)}.$$

- Boundary trajectories interpreted as moving charged particles
[Kitaev '16]
- Interaction is an attractive force for $g > 0$



Work in progress

- How much can we open the wormhole?
 - Traversability in different geometries
 - Study dependence on charge and angular momentum

Rotating BTZ

Metric:

$$ds^2 = -f^2(r)dt^2 + \frac{dr^2}{f(r)} + r^2 \left[N^\phi(r)dt + d\phi \right]^2,$$

$$f^2(r) = -M + \left(\frac{r}{\ell}\right)^2 + \frac{J^2}{4r^2}, \quad N^\phi(r) = \frac{J}{2} \frac{r^2 - r_+^2}{r^2 r_+^2}.$$

$$r_{\pm} = \ell \sqrt{\frac{M}{2} \left(1 \pm \sqrt{1 - \left(\frac{J}{M\ell}\right)^2} \right)},$$

Work in progress

Deformations of AdS_2

- Include a Φ^2 potential

$$I = \frac{1}{16\pi G_N} \left[\int d^2x \sqrt{g} [\Phi(R+2) + \alpha\Phi^2] + 2 \int_{bdy} \Phi_b K \right]$$

- $\alpha \sim 1/N$
- Geometry will be no longer AdS_2
- Connection with non-local term that appear in SYK model
[Josephine Suh, Kitaev]

Summary

- Adding a coupling between the two copies of the thermofield double yields the wormhole traversable
- Consistent with energy conditions
- Information passing through the wormhole
- Explore traversability in different scenarios. E.g.: rotating BTZ, deformations of AdS_2